Write and Solve Equations

I Can use the properties of equality and the Distributive Property to solve an equation with the variable on both sides.

Spark Your Learning

Lynn and Anna are joggers who use the same running trail.

- Anna starts jogging 3 minutes earlier.
- Lynn's average jogging speed is 0.2 mile per hour faster.
- Lynn and Anna jog at the same average speed.

Complete Part A as an entire class. Then complete Parts B–D in small groups.

A. What mathematical question can you ask about this situation? What information would you need to know to answer your question?

B. What variable(s) are involved in this situation? What unit of measurement would you use for each variable?

C. How would you use the information in the photo and the additional information your teacher gave you to answer your question? What is the answer?

D. Does your answer make sense in the context of the situation? How do you know?

Turn and Talk Predict how your answer would change for each of the following changes in the situation:

- Anna starts jogging 3 minutes earlier.
- Lynn's average jogging speed is 0.2 mile per hour faster.
- Lynn and Anna jog at the same average speed.
Build Understanding

Investigate Properties of Equality

An equation is a mathematical statement comparing two expressions using the symbol =. When you solve an equation, the solution produces a true statement when substituted for the variable in the equation. Solving an equation involves using properties of equality to write simpler equivalent equations, which all have the same solution as the original equation. In the Symbols column of the table below, \( a \), \( b \), and \( c \) are real numbers.

<table>
<thead>
<tr>
<th>Properties of Equality</th>
<th>Words</th>
<th>Symbols</th>
</tr>
</thead>
<tbody>
<tr>
<td>Addition Property of Equality</td>
<td>Adding the same number to both sides of an equation produces an equivalent equation.</td>
<td>If ( a = b ), then ( a + c = b + c ). Example: If ( x - 2 = 3 ), then ( x - 2 + 2 = 3 + 2 ).</td>
</tr>
<tr>
<td>Subtraction Property of Equality</td>
<td>Subtracting the same number from both sides of an equation produces an equivalent equation.</td>
<td>If ( a = b ), then ( a - c = b - c ). Example: If ( x + 4 = -1 ), then ( x + 4 - 4 = -1 - 4 ).</td>
</tr>
<tr>
<td>Multiplication Property of Equality</td>
<td>Multiplying both sides of an equation by the same nonzero number produces an equivalent equation.</td>
<td>If ( a = b ) and ( c \neq 0 ), then ( ac = bc ). Example: If ( \frac{x}{3} = 2 ), then ( \frac{x}{3} \cdot 3 = 2 \cdot 3 ).</td>
</tr>
<tr>
<td>Division Property of Equality</td>
<td>Dividing both sides of an equation by the same nonzero number produces an equivalent equation.</td>
<td>If ( a = b ) and ( c \neq 0 ), then ( \frac{a}{c} = \frac{b}{c} ). Example: If ( -2.5x = 10 ), then ( -\frac{2.5x}{-2.5} = \frac{10}{-2.5} ).</td>
</tr>
</tbody>
</table>

1. **A.** Using a spreadsheet, create a table like the one shown for the equation \( x = -1 \). The formula in cell B2 is an if-then-else statement that checks the value in cell A2. Fill down the formula from cell B2 to cell B8. What do you observe?

<table>
<thead>
<tr>
<th>A</th>
<th>B</th>
<th>C</th>
<th>D</th>
<th>E</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td></td>
<td>Is ( x ) a solution?</td>
<td>YES</td>
<td>NO</td>
</tr>
<tr>
<td>2</td>
<td>-3</td>
<td>NO</td>
<td></td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>-2</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>-1</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>0</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>1</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>7</td>
<td>2</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>8</td>
<td>3</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

   If the number in cell A2 equals \(-1\), then the word YES is shown in cell B2. Otherwise, the word NO is shown in cell B2.

2. **B.** Suppose you use the Multiplication Property of Equality to rewrite the equation \( x = -1 \) as \( 2x = -2 \). Use the new equation in if-then-else statements you enter in cells C2 through C8. What do you observe?

3. **C.** Suppose you use the Addition Property of Equality to rewrite the equation \( 2x = -2 \) as \( 2x + 3 = 1 \). Use the new equation in if-then-else statements you enter in cells D2 through D8. What do you observe?

**Turn and Talk** You used properties of equality to build the equation \( 2x + 3 = 1 \) from \( x = -1 \). How can you use properties of equality to solve the equation \( 2x + 3 = 1 \)?
Step It Out

Solve Equations Using the Distributive Property

Previously, you solved one-step and two-step equations. Now you will solve multistep equations. Such equations may contain grouping symbols. In order to free the terms in an equation that contains grouping symbols, you can use the Distributive Property.

The steps for solving the equation $5(2x - 3) + 4 = -6$ and checking the solution are shown below, but the steps have been scrambled.

A. Write the solution steps in the correct order.

<table>
<thead>
<tr>
<th>Step</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$10x - 11 = -6$</td>
<td></td>
</tr>
<tr>
<td>$x = 0.5$</td>
<td></td>
</tr>
<tr>
<td>$10x - 15 + 4 = -6$</td>
<td></td>
</tr>
<tr>
<td>$5(2x - 3) + 4 = -6$</td>
<td></td>
</tr>
<tr>
<td>$10x = 5$</td>
<td></td>
</tr>
</tbody>
</table>

B. Write the check steps in the correct order.

<table>
<thead>
<tr>
<th>Step</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$-6 = -6$</td>
<td></td>
</tr>
<tr>
<td>$5(2(0.5) - 3) + 4 = -6$</td>
<td></td>
</tr>
<tr>
<td>$5(-2) + 4 = -6$</td>
<td></td>
</tr>
<tr>
<td>$5(1 - 3) + 4 = -6$</td>
<td></td>
</tr>
<tr>
<td>$-10 + 4 = -6$</td>
<td></td>
</tr>
</tbody>
</table>

Turn and Talk Can you solve the equation $5(2x - 3) + 4 = -6$ without using the Distributive Property as one of the steps? Show how or explain why not.

Recall that the Distributive Property also allows you to combine like terms.

The steps for solving the equation $-2x + \frac{1}{2}(6x - 5) = \frac{3}{2}$ are shown, but some justifications are missing.

- $-2x + \frac{1}{2}(6x - 5) = \frac{3}{2}$  
  Given equation

- $-2x + 3x - \frac{5}{2} = \frac{3}{2}$  
  A. What property justifies rewriting $\frac{1}{2}(6x - 5)$ as $3x - \frac{5}{2}$?

- $(-2 + 3)x - \frac{5}{2} = \frac{3}{2}$  
  B. What property justifies rewriting $-2x + 3x$ as $(-2 + 3)x$?

- $x - \frac{5}{2} = \frac{3}{2}$  
  Simplify the coefficient of $x$.

- $x = 4$  
  C. What property justifies adding $\frac{5}{2}$ to each side of the equation?

Turn and Talk Is it possible to eliminate the fractions as a first step in solving the equation $-2x + \frac{1}{2}(6x - 5) = \frac{3}{2}$? Show how or explain why not.

Module 2 • Lesson 2.2
Solve Equations with the Variable on Both Sides

When a variable appears on both sides of an equation, you can use the Addition Property of Equality or the Subtraction Property of Equality to move the variable from one side to the other. Doing so allows you to isolate the variable on one side.

The steps for solving the equation $4(x + 1) + 1 = -3(x + 3)$ are shown, but some justifications are missing.

$$4(x + 1) + 1 = -3(x + 3) \quad \text{Given equation}$$

$$4x + 4 + 1 = -3x - 9 \quad \text{Combine constants.}$$

$$4x + 5 = -3x - 9 \quad ?$$

$$4x + 5 + 3x = -3x - 9 + 3x \quad ?$$

$$7x + 5 = -9 \quad \text{Combine like terms.}$$

$$7x = -14 \quad ?$$

$$x = -2 \quad \text{Division Property of Equality}$$

A. What property lets you rewrite each side without grouping symbols?

B. What property justifies adding $3x$ to each side?

C. What property justifies subtracting 5 from each side?

Turn and Talk  How is solving $4(x + 1) + 1 = 4(x + 3)$ different from solving $4(x + 1) + 1 = -3(x + 3)$? What is different about solving $4(x + 1) + 8 = 4(x + 3)$?

Use an Equation to Solve a Real-World Problem

When solving a real-world problem, you may have to use a formula, such as the formula $P = 2\ell + 2w$ for the perimeter of a rectangle or the formula $d = rt$ for the distance traveled at a constant rate. When using a formula, you should pay attention to the units of measurement associated with the variables to ensure that the units are consistent.

$\text{Perimeter} \ ? = 2 \cdot \text{Length (meters)} + 2 \cdot \text{Width} \ ?$

Since the length is in meters, the width must also be in meters so you can add the units on the right side. This means the perimeter is in meters because meters + meters = meters.

$\text{Distance (feet)} \ = \ \text{Rate} \ ? \cdot \text{Time (seconds)}$

For the units to be consistent in this equation, the rate must be measured in feet per second and not, say, miles per hour.
Two friends, Jon and Josh, live at opposite ends of a trail. They bike toward each other at the speeds shown. At what distance along the trail, measured from Jon’s starting point, do the two friends meet?

Use a verbal model.
Although you are asked to find distance, you will do so by expressing distance in terms of time. Note that the units miles per hour and minutes are incompatible. So, let \( t \) represent the time in hours that Jon spends biking.

\[
\begin{align*}
\text{Jon's distance (mi)} & = 15 \cdot t \\
\text{Josh's distance (mi)} & = 12 \left( t + \frac{1}{3} \right)
\end{align*}
\]

Write an equation.
\[
15t + 12 \left( t + \frac{1}{3} \right) = 22
\]

Solve the equation.
\[
\begin{align*}
15t + 12t + 4 & = 22 \\
27t + 4 & = 22 \\
27t & = 18 \\
t & = \frac{18}{27} = \frac{2}{3}
\end{align*}
\]

Answer the question.
The two friends will meet at a distance of \( 15 \left( \frac{2}{3} \right) = \) miles from Jon’s starting point on the trail.

Turn and Talk  Suppose the trail in Task 5 is only 3 miles long. Write and solve a new equation to find the time Jon spends biking. Does your solution make sense? Explain.

Module 2 • Lesson 2.2
Check Understanding

1. Which two of the equations shown below are equivalent? Explain your reasoning.

   \[ 2x + 7 = 1 \quad \text{and} \quad -3x + 4 = 12 \quad \text{and} \quad x = -3 \]

Solve each equation. Justify your solution steps, and check each solution.

2. \[ 6(2x - 5) - 8 = 4 \]
3. \[ \frac{1}{2}(4x - 3) = \frac{3}{4}(4x - 5) \]

4. Membership at the local art center is $60 per year. If you are a member, you can take lessons at the center for $7 each. If you are not a member, lessons cost $10 each. For how many lessons is the total cost with a membership the same as the total cost of lessons without a membership?

On Your Own

5. **Critique Reasoning** Mark solved the equation \( \frac{2}{3}x = 9 \) by using the Division Property of Equality to get \( x = 6 \). Did Mark solve the equation correctly? Explain why or why not.

6. **Use Repeated Reasoning** Melissa used the information shown at the right and the guess and check method to find the manager’s new pay rate after being promoted.

   A. Melissa’s work is shown in the table below. Explain how she can generalize what she has done by defining a variable and then writing and solving an equation using that variable.

<table>
<thead>
<tr>
<th>New pay rate guess</th>
<th>Calculated new weekly pay</th>
<th>Calculated old weekly pay</th>
<th>Calculated increase in weekly pay</th>
</tr>
</thead>
<tbody>
<tr>
<td>$12.00 per hour</td>
<td>$35\times$12.00 = $420.00</td>
<td>$30\times$12.00 - $4.00 = $240.00</td>
<td>$420.00 - $240.00 = $180.00 \times \n</td>
</tr>
</tbody>
</table>

B. Suppose the question had been, “What was the manager’s old pay rate?” Define the variable in a way that will answer this question. Then write and solve a new equation to show that you get a solution that is consistent with the one from Part A.
Solve each equation. Justify your solution steps, and check each solution.

7. \[4(3x - 10) + 7 = 15\]
8. \[6 - 5(2x + 1) = 21\]
9. \[2 - \frac{3}{4}(8x - 6) = 11\]
10. \[0.2(4 - 5x) + 1 = 2.4\]
11. \[5(x + 1) - 2(3x - 4) = 14\]
12. \[2(5 - x) + 3(4x - 1) = -6\]
13. \[4x - 3 = 7x + 6\]
14. \[-2x + 5 = 3x + 1\]
15. \[5(2x + 3) - 7 = -2(x + 2)\]
16. \[8 - 3(2x - 5) = 4(x + 2)\]
17. \[0.4(2x + 3) = 0.3x + 0.8\]
18. \[\frac{1}{2}(6x - 5) = x - \frac{3}{2}\]

19. **Financial Literacy**  Kiera recently bought a used car from a relative, who agreed to let her pay for the car over time. She also borrowed money from her parents for a summer internship in Washington, D.C. She is paying off both loans in equal weekly payments. Use the information in the photos to determine how many weeks it takes for the balances of the loans to be the same.

   ![Image of car and Capitol Building]

   **Use Structure**  Jan noticed that the equation \[3(4x - 7) + 2(4x - 7) = 5\] has the form \[3\underline{\quad} + 2\underline{\quad} = 5\] where \[\underline{\quad} = 4x - 7\]. Explain how Jan can use this observation to solve the equation. Then use the same method to solve the equation \[2(3x + 4) - 5(3x + 4) = 33\].

20. **Open Ended**  Write an equation that can be solved using the Subtraction Property of Equality and the Division Property of Equality. Show another way to solve the same equation using the Addition Property of Equality and the Multiplication Property of Equality. Explain your reasoning.

21. Two subscription services offer deliveries of boxes of nutritious, organic snack foods each month. For how many months of deliveries will the two plans cost the same?

   **SNACKS 4 U**
   - Pay just $4 per month for the first 3 months of deliveries.
   - Then pay $14 per month for deliveries after the third month.
   - Get 1 free month of deliveries.
   - Then pay $10 per month for deliveries after the first month.

   **HEALTHY TIMES**

Module 2 • Lesson 2.2
23. Dan and Luke begin running on a track at the same time and from the same starting point. Dan’s average speed is 4.5 m/s, while Luke’s average speed is 5.1 m/s. Dan’s running lane is shorter than Luke’s lane, as shown. Because Luke runs faster, he will eventually meet up with Dan but be 1 lap ahead of him. How far will Luke have run when this happens?

24. **Reason** Consider the equation 
   \[3(2x - 5) = ax + b\] where \(a\) and \(b\) represent constants.
   
   A. For what values of \(a\) and \(b\) would any value of \(x\) be a solution of the equation? Explain your reasoning.
   
   B. For what values of \(a\) and \(b\) would the equation not have any solutions? Explain your reasoning.
   
   C. For what values of \(a\) and \(b\) would the equation have exactly one solution?

25. **Open Middle** Using the integers from –9 to 9 at most one time each, replace the boxes to create an equation that has a positive solution. Then repeat this activity to create a second equation that has a negative solution.

26. Which expressions are equivalent to \(4x^3y^2\)? Select all that apply.
   
   A. \((2xy)^2\)  
   B. \(2x^2y^6 + 2xy^6\)  
   C. \(2xy^3 + 2xy^6\)  
   D. \((16x^2y^2)^\frac{1}{2}\)  
   E. \((2x^2y^6)^\frac{1}{2}\)  

27. A circular mulch bed has a radius of 1.6 feet. A bag of mulch contains 2 cubic feet of mulch. If all of the mulch is spread evenly on the bed, what is the mulch’s depth to an appropriate number of significant digits?

   A. 0.2 foot  
   B. 0.25 foot  
   C. 0.249 foot  
   D. 0.2487 foot

28. To make salsa, you buy 8 tomatoes that weigh \(t\) pounds and that cost $2.20 per pound. You also buy 2 peppers that weigh \(p\) pounds and that cost $3.40 per pound. Which expression gives the total cost (in dollars) of the items?

   A. 2.2\(t\)  
   B. 3.4\(p\)  
   C. 2.2\(t\) + 3.4\(p\)  
   D. 17.6\(t\) + 6.8\(p\)

29. Which formulas can be used to find the perimeter \(P\) of a rectangle with length \(\ell\) and width \(w\)? Select all that apply.

   A. \(P = \ell + w\)  
   B. \(P = \ell w\)  
   C. \(P = 2\ell + 2w\)  
   D. \(P = (2\ell)(2w)\)  
   E. \(P = 2(\ell + w)\)  
   F. \(P = 4\ell w\)

I’m in a **Learning Mindset**!

What properties did I learn to use to justify the steps in solving an equation?
**2.2 Write and Solve Equations**

**LESSON FOCUS AND COHERENCE**

**Mathematics Standards**
- Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.
- Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.

**Mathematical Practices and Processes**
- Use appropriate tools strategically.
- Look for and make use of structure.
- Model with mathematics.

**I Can Objective**
I can use the properties of equality and the Distributive Property to solve an equation with the variable on both sides.

**Learning Objective**
Solve linear equations with grouping symbols or with the variable on both sides, and use linear equations to model and solve real-world problems.

**Language Objective**
Explain the steps needed to solve a linear equation with grouping symbols or with the variable on both sides.

**Vocabulary**
- Review: equation, equivalent equations, solution of an equation in one variable
- Lesson Materials: spreadsheet software

**Mathematical Progressions**

<table>
<thead>
<tr>
<th>Prior Learning</th>
<th>Current Development</th>
<th>Future Connections</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Students:</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>• wrote and interpreted algebraic expressions that represent real-world quantities. (2.1)</td>
<td>• solve linear equations with grouping symbols or with the variable on both sides.</td>
<td>• will solve linear equations with coefficients represented by letters. (2.3)</td>
</tr>
<tr>
<td>• wrote and solved equations of the form $px + q = r$ and $p(x + q) = r$ where $p$, $q$, and $r$ are specific rational numbers. (Gr7, 7.3 and 7.4)</td>
<td>• explain and justify each step required to solve a linear equation.</td>
<td>• will write and solve linear inequalities. (2.4 and 2.5)</td>
</tr>
<tr>
<td>• use linear equations to represent and solve real-world problems.</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**PROFESSIONAL LEARNING**

**Visualizing the Math**
Students may find it helpful to draw a bar model to represent real-world situations, such as the problem in Task 5 on page 41. The bar model at the right shows that the sum of Jon's distance and Josh's distance equals the length of the trail.

So an equation that models the problem is $15t + 12\left(t + \frac{1}{3}\right) = 22$.

<table>
<thead>
<tr>
<th>Jon's distance (mi)</th>
<th>Josh's distance (mi)</th>
<th>Length of trail (mi)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$15t$</td>
<td>$12\left(t + \frac{1}{3}\right)$</td>
<td>$22$</td>
</tr>
</tbody>
</table>
**Problem of the Day**
Mia has a $25 gift card for an online music store. She buys an album for $9.50 and wants to use the remaining money on the card to buy individual songs, which cost $1.25 each. Write and solve an equation to find the number of songs Mia can buy. Let $x$ represent the number of songs; $9.50 + 1.25x = 25; x = 12.4; Mia can buy 12 songs.

**Make Connections**
Based on students’ responses to the Problem of the Day, choose one of the following:

1. Project the Interactive Reteach, Grade 7, Lesson 7.4.
2. Complete the Prerequisite Skills Activity:

   - Students work in pairs. One student should write an expression of the form $px + q$, such as $-2x + 3$. The other student should write a constant $r$, such as 15. Have the two students work together to solve the equation $px + q = r$ and justify each step of their solution method. Then have them switch roles to create and solve a different equation.

   - Think about the equation $-2x + 3 = 15$. What is the first step for solving this equation? What property do you use for this step? Subtract 3 from each side; Subtraction Property of Equality

   - What equation do you get when you subtract 3 from each side of $-2x + 3 = 15$? $-2x = 12$

   - What is the next step for solving the equation? What property do you use? Divide each side by $-2$; Division Property of Equality

   - What is the solution of the equation? How can you check the solution? $-6$; Substitute $-6$ for $x$ in the original equation $-2x + 3 = 15$ and verify that you get a true statement.

   If students continue to struggle, use Tier 2 Skill 3.

**Vocabulary Review**
Objective: Students demonstrate an understanding of equivalent equations.

Materials: index cards

Have students work in small groups. On half of the index cards, write a two-step equation. On the other cards, write a one-step equation, such that some of the one-step equations are equivalent to one or more of the two-step equations. Give each group a set of each type of card. Ask students to find any equivalent equation pairs in the index cards they are given. Encourage students to explain in their own words what it means for equations to be equivalent.
Small-Group Options
Use these teacher-guided activities with pulled small groups.

**On Track**

**Materials:** index cards

Give each student a card with a linear expression such as $2x + 4$ or $5(3x + 2)$ written on it. Have students pair up and solve the equation formed by setting their expressions equal to each other. Each student should pair up with as many other students as time allows.

```
2x + 4
5(3x + 2)
```

**Almost There**

**Materials:** algebra tiles

Write the equation $3(x + 2) + 1 = 13$. Have students do the following:

- Model the equation with algebra tiles, using three groups of one $x$-tile and two 1-tiles to represent $3(x + 2)$.
- Use the model to write an equivalent equation without grouping symbols.
- Solve the equation by performing the same operation on each “side” of the model, such as adding tiles to or removing tiles from each side. Continue until you have an $x$-tile by itself on one side and only 1-tiles on the other side. After each step, write the corresponding equation.
- Review your solution steps. Then solve the equation $4(x - 5) - 7 = -9$ without using algebra tiles.

**Ready for More**

Write the equation $2(x + a) = bx + 8$. Have students find values of $a$ and $b$ for which the following are true:

- The equation has infinitely many solutions.
- The equation has no solution.
- The equation has $-3$ as its only solution.

Math Center Options
Use these student self-directed activities at centers or stations.

**On Track**

- Interactive Digital Lesson
- Journal and Practice Workbook
- Interactive Glossary: equation, equivalent equations, solution of an equation in one variable
- Module Performance Task: Spies and Analysts

**Almost There**

- Reteach 2.2
- Interactive Reteach 2.2
- Rti Tier 2 Skill 3: Solve Two-Step Equations

**Ready for More**

- Challenge 2.2
- Interactive Challenge 2.2

**Unit Project**
Check students’ progress by asking what equation they wrote to find the amount of water needed to dilute the solution.
During the Spark Your Learning, listen and watch for strategies students use. See samples of student work on this page.

### Use an Equation

Let \( t \) = Lynn’s jogging time in hours.
Let \( t - 0.1 \) = Anna’s jogging time in hours.

\[
5.4t = L(t - 0.1) \\
5.4t = L t - 0.6 \\
-0.6t = -0.6 \\
t = 1
\]

Anna catches up with Lynn 1 hour after Lynn starts jogging, or at 5:00 p.m.

### Use a Table

Let \( t \) = time after 4:00 p.m. in hours.

<table>
<thead>
<tr>
<th>( t )</th>
<th>Lynn’s Distance (mi)</th>
<th>Anna’s Distance (mi)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>0.1</td>
<td>5.4(0.1) = 0.54</td>
<td>0</td>
</tr>
<tr>
<td>0.2</td>
<td>5.4(0.2) = 1.08</td>
<td>( L(0.2 - 0.1) = 0.6 )</td>
</tr>
<tr>
<td>0.5</td>
<td>5.4(0.5) = 2.7</td>
<td>( L(0.5 - 0.1) = 2.4 )</td>
</tr>
<tr>
<td>0.8</td>
<td>5.4(0.8) = 4.32</td>
<td>( L(0.8 - 0.1) = 4.2 )</td>
</tr>
<tr>
<td>0.9</td>
<td>5.4(0.9) = 4.86</td>
<td>( L(0.9 - 0.1) = 4.8 )</td>
</tr>
<tr>
<td>1</td>
<td>5.4(1) = 5.4</td>
<td>( L(1 - 0.1) = 5.4 )</td>
</tr>
</tbody>
</table>

Anna catches up with Lynn 1 hour after 4:00 p.m., or at 5:00 p.m.

### COMMON ERROR: Uses Wrong Units

Let \( t \) = Lynn’s jogging time in hours.
Let \( t - \omega \) = Anna’s jogging time in hours.

\[
5.4t = L(t - \omega) \\
5.4t = L t - 3\omega \\
-0.6t = -3\omega \\
t = 60
\]

Anna catches up with Lynn 60 hours after Lynn starts jogging.

If students . . . use an equation to solve the problem, they are employing an efficient method and demonstrating an exemplary understanding of writing and solving linear equations from Grade 8.

Have these students . . . explain how they determined their equation and how they solved it. Ask:

- How did you use the given information and the relationship between speed, time, and distance to write your equation?
- What properties did you use to solve your equation?

If students . . . use a table to solve the problem, they understand how the quantities in the problem are related but may not know how to model the problem algebraically.

Activate Prior Knowledge . . . by having students write algebraic expressions for the distances jogged by Lynn and Anna. Ask:

- How can you write expressions with a variable for the distances that Lynn and Anna jog?
- What is true about your expressions when Anna catches up with Lynn?

If students . . . do not convert 6 minutes to 0.1 hour when writing an expression for Anna’s jogging time, they may not understand that the same units for time must be used for all quantities in the equation.

Then intervene . . . by pointing out that since the problem gives time in different units, students must convert times to a common unit. Ask:

- The speeds in the problem are given in miles per hour. If you use these speeds in your equation, in what units must you express the jogging times?
- If you calculate that Anna takes 60 hours to catch up with Lynn, why might you think you have made a mistake?
Write and Solve Equations

I Can use the properties of equality and the Distributive Property to solve an equation with the variable on both sides.

Spark Your Learning

Lynn and Anna are joggers who use the same running trail.

Complete Part A as an entire class. Then complete Parts B–D in small groups.

A. What mathematical question can you ask about this situation? What information would you need to know to answer your question?
B. What variable(s) are involved in this situation? What unit of measurement would you use for each variable?  Possible answer: time; hours
C. How would you use the information in the photo and the additional information your teacher gave you to answer your question? What is the answer?  See Strategy 1 on the facing page.
D. Does your answer make sense in the context of the situation? How do you know?  Possible answer: One hour is a reasonable amount of time for a person to jog.

Turn and Talk  Predict how your answer would change for each of the following changes in the situation:  See margin.
• Anna starts jogging 3 minutes earlier
• Anna’s average jogging speed is 0.2 mile per hour faster
• Lynn and Anna jog at the same average speed

CULTIVATE CONVERSATION  •  Co-Craft Questions

If students have difficulty formulating a mathematical question about the situation in the Spark Your Learning, ask them to visualize themselves running after a friend who is ahead of them but moving at a slower speed. What are some natural questions to ask about this situation?

Work together to craft the following questions:
• Will Anna catch up with Lynn?
• How much time will it take Anna to catch up with Lynn?
• What distance will Anna and Lynn have traveled when Anna catches up with Lynn?

Then have students think about what additional information, if any, they would need to answer these questions. Ask:
• Can you determine when Anna catches up with Lynn if you know only the joggers’ speeds? Why or why not?
• Can you determine when Anna catches up with Lynn if you know only the time at which each person started jogging? Explain.

EL

BUILD SHARED UNDERSTANDING

Select groups of students who used various strategies and have them share with the class how they solved the problem. Encourage students to ask questions of each other. Make sure students understand that since the joggers’ speeds are given in miles per hour, the jogging times must be expressed in hours. This means that the difference between Lynn’s and Anna’s starting times, 6 minutes, must be converted to 0.1 hour.
Build Understanding

**Investigate Properties of Equality**

An equation is a mathematical statement comparing two expressions using the symbol =. When you solve an equation, the solution produces a true statement when substituted for the variable in the equation. Solving an equation involves using properties of equality to write simpler equivalent equations, which all have the same solution as the original equation. In the Symbols column of the table below, a, b, and c are real numbers.

<table>
<thead>
<tr>
<th>Properties of Equality</th>
<th>Words</th>
<th>Symbols</th>
</tr>
</thead>
<tbody>
<tr>
<td>Addition Property of Equality</td>
<td>Adding the same number to both sides of an equation produces an equivalent equation.</td>
<td>If ( a = b ), then ( a + c = b + c ). Example: If ( x = 3 ), then ( x - 2 + 3 = 3 + 2 ).</td>
</tr>
<tr>
<td>Subtraction Property of Equality</td>
<td>Subtracting the same number from both sides of an equation produces an equivalent equation.</td>
<td>If ( a = b ), then ( a - c = b - c ). Example: If ( x + 4 = -1 ), then ( x + 4 - 4 = -1 - 4 ).</td>
</tr>
<tr>
<td>Multiplication Property of Equality</td>
<td>Multiplying both sides of an equation by the same nonzero number produces an equivalent equation.</td>
<td>If ( a = b ) and ( c \neq 0 ), then ( ac = bc ). Example: If ( \frac{2}{3} = \frac{4}{6} ), then ( \frac{2}{3} \cdot 3 = \frac{4}{6} \cdot 3 ).</td>
</tr>
<tr>
<td>Division Property of Equality</td>
<td>Dividing both sides of an equation by the same nonzero number produces an equivalent equation.</td>
<td>If ( a = b ) and ( c \neq 0 ), then ( \frac{a}{c} = \frac{b}{c} ). Example: If ( \frac{-2x}{5} = \frac{-10}{5} ), then ( -\frac{2x}{5} \cdot 5 = \frac{-10}{5} \cdot 5 ).</td>
</tr>
</tbody>
</table>

**Example:**

A. Using a spreadsheet, create a table like the one shown for the equation \( x = -1 \). The formula in cell B2 is an if-then-else statement that checks the value in cell A2. Fill down the formula from cell B2 to cell B8. What do you observe?

B. Suppose you use the Multiplication Property of Equality to rewrite the equation \( x = -1 \) as \( 2x = -2 \). Use the new equation in if-then-else statements you enter in cells C2 through C8. What do you observe?

C. Suppose you use the Addition Property of Equality to rewrite the equation \( 2x = -2 \) as \( 2x + 3 = 1 \). Use the new equation in if-then-else statements you enter in cells D2 through D8. What do you observe?

**Turn and Talk** You used properties of equality to build the equation \( 2x + 3 = 1 \). How can you use properties of equality to solve the equation \( 2x + 3 = 1 \)? See margin.

### LEVELED QUESTIONS

<table>
<thead>
<tr>
<th>Depth of Knowledge (DOK)</th>
<th>Leveled Questions</th>
<th>What Does This Tell You?</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Level 1</strong> Recall</td>
<td>What property allows you to subtract 1 from each side of ( 3x + 1 = -5 ) to obtain the equivalent equation ( 3x = -6 )? <strong>Subtraction Property of Equality</strong></td>
<td>Students’ answers will indicate whether they understand the meaning of one of the properties of equality.</td>
</tr>
<tr>
<td><strong>Level 2</strong> Basic Application of Skills &amp; Concepts</td>
<td>How can you solve the equation ( 3x + 1 = -5 )? I can use the Subtraction Property of Equality to subtract 1 from each side, giving ( 3x = -6 ). Then I can use the Division Property of Equality to divide each side by 3, giving the solution ( x = -2 ).</td>
<td>Students’ answers will demonstrate whether they can use the properties of equality to solve a two-step equation.</td>
</tr>
<tr>
<td><strong>Level 3</strong> Strategic Thinking &amp; Complex Reasoning</td>
<td>How can you show that ( 3x + 1 = -5 ) and ( 4x + 3 = -9 ) are not equivalent equations? Possible answer: I can solve ( 3x + 1 = -5 ) to get ( x = -2 ) and ( 4x + 3 = -9 ) to get ( x = -3 ). The solutions are different, so, the equations are not equivalent.</td>
<td>Students’ answers will reflect whether they understand the meaning of equivalent equations and can reason strategically about how to determine whether two equations are equivalent.</td>
</tr>
</tbody>
</table>
Step It Out

Solve Equations Using the Distributive Property

Previously, you solved one-step and two-step equations. Now you will solve multi-step equations. Such equations may contain grouping symbols. In order to free the terms in an equation that contains grouping symbols, you can use the Distributive Property.

2 The steps for solving the equation $5(2x - 3) + 4 = -6$ and checking the solution are shown below, but the steps have been scrambled.

<table>
<thead>
<tr>
<th>A. Write the solution steps in the correct order.</th>
<th>B. Write the check steps in the correct order.</th>
</tr>
</thead>
<tbody>
<tr>
<td>$10x - 11 = -6$</td>
<td>$-6 = -6$</td>
</tr>
<tr>
<td>$x = 0.5$</td>
<td></td>
</tr>
<tr>
<td>$10x - 15 + 4 = -6$</td>
<td>$5(2(0.5) - 3) + 4 = -6$</td>
</tr>
<tr>
<td>$5(2x - 3) + 4 = -6$</td>
<td>$5(-2) + 4 = -6$</td>
</tr>
<tr>
<td>$10x = 5$</td>
<td>$-10 + 4 = -6$</td>
</tr>
</tbody>
</table>

A. B. See Additional Answers.

Turn and Talk  Can you solve the equation $5(2x - 3) + 4 = -6$ without using the Distributive Property as one of the steps? Show how or explain why not.  See margin.

Recall that the Distributive Property also allows you to combine like terms.

3 The steps for solving the equation $-2x + \frac{1}{2}(6x - 5) = \frac{3}{2}$ are shown, but some justifications are missing.

-2x + \frac{1}{2}(6x - 5) = \frac{3}{2}  \hspace{1cm} \text{Given equation}

-2x + 3x - \frac{5}{2} = \frac{3}{2}  \hspace{1cm} A. Distributive Property

\frac{1}{2} = \frac{1}{2}  \hspace{1cm} ?

-2x + 3x = \frac{3}{2}  \hspace{1cm} B. What property justifies rewriting -2x + 3x as 3x - \frac{5}{2}?

\frac{1}{2} = \frac{1}{2}  \hspace{1cm} ?

x = \frac{3}{2}  \hspace{1cm} C. What property justifies adding \frac{1}{2} to each side of the equation?

x = 4  \hspace{1cm} C. Addition Property of Equality

Turn and Talk  Is it possible to eliminate the fractions as a first step in solving the equation $-2x + \frac{1}{2}(6x - 5) = \frac{3}{2}$? Show how or explain why not.  See margin.

Step It Out

Task 2 Use Structure  Encourage students to use the structure of addition to check whether the Distributive Property works for subtraction.

By writing subtraction as adding the opposite of a number, students can demonstrate that the Distributive Property holds for a product of a number and a difference of two numbers:

$a(b - c) = a[b + (-c)] = ab + a(-c) = ab - ac$

Sample Guided Discussion:

Q What will be the last equation in the sequence of solution steps? Why? The equation $x = 0.5$ will be last because it is the only equation that has the variable by itself on one side.

Q Why do you substitute the solution you found into the original equation to check your work? Possible answer: I could have made a mistake when solving the original equation. If so, some of my intermediate equations may contain errors.

Task 3 Use Structure  Encourage students to use the structure of the Distributive Property and the properties of equality to justify each step in the solution.

Sample Guided Discussion:

Q On the left side of the second equation, why is $\frac{5}{2}$ instead of 5 being subtracted? When you use the Distributive Property to rewrite $\frac{1}{2}(6x - 5)$, you must multiply both terms inside the parentheses by $\frac{1}{2}$, not just the first term.

Turn and Talk  Help students realize that they can eliminate the fractions from an equation by multiplying each side by the LCD of the fractions. Yes; I can multiply both sides of the equation by 2 to eliminate the fractions. This gives the equation $-4x + 6x - 5 = 3$. 

Module 2 • Lesson 2.2

PROFICIENCY LEVEL

Beginning
Write the terms $-2x$ and $3x$. Say,“These are like terms because each term has the same variable, $x$, raised to the same power—the first power.” Then write the term $4m^2$ and ask students to write a like term for $4m^2$.

Intermediate
Have students work in groups. Give each group a set of index cards. Each card should show two terms, such as $5x$ and $-3x$ or $6y^2$ and $6y^2$. Ask students to explain why the terms on each card either are or are not like terms.

Advanced
Have students explain how to use the Distributive Property to combine like terms.

Lesson 2.2
Task 4  **Use Structure**  Students use properties of equality to isolate the variable on one side of an equation.

Point out to students that when solving an equation with the variable on both sides, they can isolate the variable on either the left or right side. Some students may prefer always to isolate the variable on the left side. Others may find it helpful to choose the side that makes the coefficient of the variable be positive when the variable term is isolated on one side.

**Sample Guided Discussion:**

Q How are the first and second equations in the solution different? How does this suggest the property that was used to obtain the second equation? The first equation has parentheses while the second equation does not; this suggests that the Distributive Property was used to eliminate the parentheses.

Q For the equation $4x + 5 = -3x - 9$, what operation do you need to perform so that the variable appears only on the left side? Which property are you using? Add $3x$ to each side; Addition Property of Equality

**Turn and Talk**  The equations that students have seen so far in this lesson each have one solution. In this problem, students analyze equations that have no solution or infinitely many solutions. The original equation, $4(x + 1) + 1 = -3(x + 3)$ has one solution, $x = -2$. When I try to solve $4(x + 1) + 1 = 4(x + 3)$ for $x$, I get the false equation $5 = 12$, which means this given equation has no solution. When I try to solve $4(x + 1) + 8 = 4(x + 3)$ for $x$, I get the true equation $12 = 12$, which means that any real number is a solution of this given equation.
Two friends, Jon and Josh, live at opposite ends of a trail. They bike toward each other at the speeds shown. At what distance along the trail, measured from Jon's starting point, do the two friends meet?

Use a verbal model.
Although you are asked to find distance, you will do so by expressing distance in terms of time. Note that the units miles per hour and minutes are incompatible. So, let $t$ represent the time in hours that Jon spends biking.

<table>
<thead>
<tr>
<th>Jon's rate (mi/h)</th>
<th>Jon's time (h)</th>
<th>Josh's rate (mi/h)</th>
<th>Josh's time (h)</th>
<th>Distance (mi)</th>
</tr>
</thead>
<tbody>
<tr>
<td>15</td>
<td>$t$</td>
<td>12</td>
<td>$t + \frac{1}{3}$</td>
<td>22</td>
</tr>
</tbody>
</table>

Write an equation.

$15t + 12\left(t + \frac{1}{3}\right) = 22$

Solve the equation.

$15t + 12t + 4 = 22$
$27t + 4 = 22$
$27t = 18$
$t = \frac{2}{3}$

Answer the question.
The two friends will meet at a distance of $15\left(\frac{2}{3}\right) = \frac{7}{3}$ miles from Jon's starting point on the trail.

**Task 5 Model with Mathematics** Encourage students to use a verbal model to help them write a mathematical model for a real-world situation.

**Support Sense-Making Three Reads**
Have students read the problem three times. Use the questions below for a different focus each read.

1. What is the situation about?
2. What are the quantities in the situation?
3. What are possible mathematical questions you could ask about the situation?

Sample Guided Discussion:

- Q: What is true about the sum of Jon's biking distance and Josh's biking distance? The sum of the distances is 22 miles.
- Q: How can you express the biking distances in terms of time? You can write each distance as the product of speed and time.
- Q: How can you convert 20 minutes to hours? Possible answer: I can multiply 20 minutes by the conversion factor $\frac{1}{60}$ hour to obtain the equivalent time $\frac{1}{3}$ hour.
- Q: The solution of the equation in the problem is $t = \frac{2}{3}$ hour. Is this the answer to the question asked in the problem? Explain. No; The problem asks for the distance from Jon's starting point at which Jon and Josh meet. You need to multiply the solution of the equation by Jon's speed, 15 mi/h, to find this distance and answer the question.

**Turn and Talk** Suppose the trail in Task 5 is only 3 miles long. Write and solve a new equation to find the time Jon spends biking. Does your solution make sense? Explain. See margin.

**Turn and Talk** If students do not notice that the solution of the equation makes no sense, ask them if time can be negative. The equation would be $15t + 12\left(t + \frac{1}{3}\right) = 3$, so $27t + 4 = 3$, and $t = -\frac{1}{3}$, but time cannot be negative. So, Jon and Josh cannot be 3 miles apart when they start.
On Your Own

Assignment Guide

The chart below indicates which problems in the On Your Own are associated with each task in the Learn Together. Assign daily homework for tasks completed.

<table>
<thead>
<tr>
<th>Learn Together Tasks</th>
<th>On Your Own Problems</th>
</tr>
</thead>
<tbody>
<tr>
<td>Task 1, p. 38</td>
<td>Problems 5 and 21</td>
</tr>
<tr>
<td>Task 2, p. 39</td>
<td>Problems 7–10</td>
</tr>
<tr>
<td>Task 3, p. 39</td>
<td>Problems 11, 12, and 20</td>
</tr>
<tr>
<td>Task 4, p. 40</td>
<td>Problems 13–18, 24, and 25</td>
</tr>
<tr>
<td>Task 5, p. 41</td>
<td>Problems 6, 19, 22, and 23</td>
</tr>
</tbody>
</table>

**ANSWERS**

6.A. Let $p$ represent the manager's new pay rate. Then $p - 4$ represents the manager's old pay rate; $35p - 30(p - 4) = $197.50; $15.50 per hour

6.B. Let $p$ represent the manager's old pay rate. Then $p + 4$ represents the manager's new pay rate; $35(p + 4) - 30p = $197.50; $11.50 per hour

3 Check Understanding

Formative Assessment

Use formative assessment to determine if your students are successful with this lesson's learning objective.

Students who successfully complete the Check Understanding can continue to the On Your Own practice.

For students who miss 1 problem or more, work in a pulled small group using the Almost There small-group activity on page 37C.

4 Differentiation Options

Differentiate instruction for all students using small-group activities and math center activities on page 37C.
7-18. See Additional Answers for solution steps, justifications, and solution checks.
Solve each equation. Justify your solution steps, and check each solution.
7. \( 4(3x - 10) + 7 = 15 \) \( x = 4 \)
8. \( 6 - 5(2x + 1) = 21 \) \( x = -2 \)
9. \( 2 - \frac{3}{4}(x - 6) = 11 \) \( x = -\frac{3}{4} \)
10. \( 0.2(4 - 5x) + 1 = 2.4 \) \( x = -0.6 \)
11. \( 5(x + 1) - 2(3x - 4) = 14 \) \( x = -1 \)
12. \( 2(5 - x) + 3(4x - 1) = -6 \) \( x = -\frac{1}{3} \)
13. \( 4x - 3 = 7x + 6 \) \( x = -3 \)
14. \( -2x + 5 = 3x + 1 \) \( x = 0.8 \)
15. \( 5(2x + 3) - 7 = -2(x + 2) \) \( x = -1 \)
16. \( 8 - 3(2x - 5) = 4(x + 2) \) \( x = 1.5 \)
17. \( 0.4(2x + 3) = 0.3x + 0.8 \) \( x = -0.8 \)
18. \( \frac{3}{2}(6x - 5) = x - \frac{1}{2} \) \( x = 2 \)
19. Financial Literacy
Kiera recently bought a used car from a relative, who agreed to let her pay for the car over time. She also borrowed money from her parents for a summer internship in Washington, D.C. She is paying off both loans in equal weekly payments. Use the information in the photos to determine how many weeks it takes for the balances of the loans to be the same. 28 weeks

Questioning Strategies
Problem 19 Suppose both loans are paid off at a rate of $200 per week. Without doing any calculations, what conclusion can you draw about when the loan balances will be the same? The loan balances will never be the same. Because the $6500 loan has a larger initial balance but is paid off at the same rate as the smaller loan, the larger loan’s balance will never “catch up” with the smaller loan’s balance.

Watch for Common Errors
Problem 22 Some students may write the expressions for the subscription costs as \( 4 + 14m \) for Snacks 4 U and 10m for Healthy Times, where \( m \) is the subscription time in months. Point out that the cost of $14 per month for Snacks 4 U applies only to the amount of time over 3 months, so the correct expression for Snacks 4 U is \( 4 + 14(m - 3) \). Similarly, the cost of $10 per month for Healthy Times applies only to the amount of time after 1 month, so the correct expression for Healthy Times is \( 10(m - 1) \). Therefore, the equation for the problem is \( 4 + 14(m - 3) = 10(m - 1) \).

ANSWERS
20. For \( 3(4x - 7) + 2(4x - 7) = 5 \) \( 3\square + 2\square = 5 \) implies that \( 5\square = 5 \), or \( \square = 1 \). Since \( \square = 4x - 7 \), this means that \( 4x - 7 = 1 \), or \( 4x = 8 \), or \( x = 2 \).
   For \( 2(3x + 4) - 5(3x + 4) = 33 \) \( 2\square - 5\square = 33 \) implies that \( -3\square = 33 \), or \( \square = -11 \). Since \( \square = 3x + 4 \), this means \( 3x + 4 = -11 \), or \( 3x = -15 \), or \( x = -5 \).
21. Possible answer:
   Using Subtraction and Division: \( 3x + 4 = 13 \);
   \( 3x + 4 = 13 - 4; 3x = 9; \frac{3x}{3} = \frac{9}{3}; x = 3 \)
   Using Addition and Multiplication: \( 3x + 4 = 13 \);
   \( 3x + 4 + (-4) = 13 + (-4); 3x = 9; \frac{3x}{3} = \frac{9}{3}; x = 3 \)
5) Wrap-Up
Summarize learning with your class. Consider using the Exit Ticket, Put It in Writing, or I Can Scale.

Exit Ticket
Kyla alternates between walking and jogging on an 11-mile trail. Her walking speed is 4 mi/h, and her jogging speed is 6 mi/h. Kyla takes 2 hours to go from the beginning to the end of the trail. Write and solve an equation to find the distance Kyla walked and the distance she jogged.

4t + 6(2 - t) = 11; t = 0.5; Kyla walked 4(0.5) = 2 miles and jogged 6(2 - 0.5) = 9 miles.

Put It in Writing
Describe some strategies you can use to solve a linear equation in one variable.

I Can
The scale below can help you and your students understand their progress on a learning goal.

I can use the properties of equality and the Distributive Property to solve an equation with the variable on both sides, and I can explain my solution steps to others.

I can use the properties of equality and the Distributive Property to solve an equation with the variable on both sides.

I can use the properties of equality and the Distributive Property to solve an equation with the variable and grouping symbols on one side.

I can recognize which property of equality is being used to produce an equivalent equation in a stepped-out solution.

Spiral Review • Assessment Readiness
These questions will help determine if students have retained information taught in the past and can also prepare them for high-stakes assessments. Here, students must recognize equivalent expressions or formulas (2.1), choose a level of precision appropriate to limitations on measurement when reporting a quantity (1.3), and interpret the meaning of algebraic expressions in the context of a problem situation (2.1).

23. Dan and Luke begin running on a track at the same time and from the same starting point. Dan’s average speed is 4.5 m/s, while Luke’s average speed is 5.1 m/s. Dan’s running lane is shorter than Luke’s lane, as shown. Because Luke runs faster, he will eventually meet up with Dan but be 1 lap ahead of him. How far will Luke have run when this happens? 4080 meters

24. Consider the equation 3(2x - 5) = ax + b where a and b represent constants.
   A. For what values of a and b would any value of x be a solution of the equation? Explain your reasoning. A–C. See Additional Answers.
   B. For what values of a and b would the equation not have any solutions? Explain your reasoning.
   C. For what values of a and b would the equation have exactly one solution?

25. Open Middle™ Using the integers from −9 to 9 at most one time each, replace the boxes to create an equation that has a positive solution. Then repeat this activity to create a second equation that has a negative solution. See Additional Answers.

Spiral Review • Assessment Readiness
26. Which expressions are equivalent to 4x/y²?
   Select all that apply.
   A. (2xy)²
   B. 2x²y
   C. (16xy)²
   D. 2xy + 2xy
   E. (16xy)²

27. A circular mulch bed has a radius of 1.6 feet. A bag of mulch contains 2 cubic feet of mulch. If all of the mulch is spread evenly on the bed, what is the mulch’s depth to an appropriate number of significant digits?
   A. 0.2 foot
   B. 0.25 foot
   C. 0.249 foot
   D. 0.2487 foot

28. To make salsa, you buy 8 tomatoes that weigh t pounds and that cost $3.40 per pound. You also buy 2 peppers that weigh p pounds and that cost $2.20 per pound. You also buy 2 peppers that weigh p pounds and that cost $3.60 per pound. Which expression gives the total cost (in dollars) of the items?
   A. 2t + 3.40
   B. 2t + 3.60
   C. 2t + 3.40 + 3.60
   D. 17.6t + 6.8t

29. Which formulas can be used to find the perimeter P of a rectangle with length ℓ and width w? Select all that apply.
   A. P = ℓ + w
   B. P = 2(ℓ + w)
   C. P = ℓw
   D. P = 2ℓ + 2w
   E. P = 4ℓw

I'm in a Learning Mindset!
What properties did I learn to use to justify the steps in solving an equation?

Learning Mindset
Resilience Monitors Knowledge and Skills
Point out that making sure a given step in solving a problem follows logically from the previous step is essential in all areas of mathematics, not just when solving equations. Encourage students to develop the habit of justifying the steps of their solutions when solving any mathematical problem. Also let students know that although they used the Distributive Property and the properties of equality to solve only linear equations in this lesson, they will use these properties to solve other types of equations later in the course. How does justifying each step when solving a mathematical problem help you have a more confident mindset? When you can’t think of a good justification for one of your solution steps, what might that suggest about your approach to solving the problem?